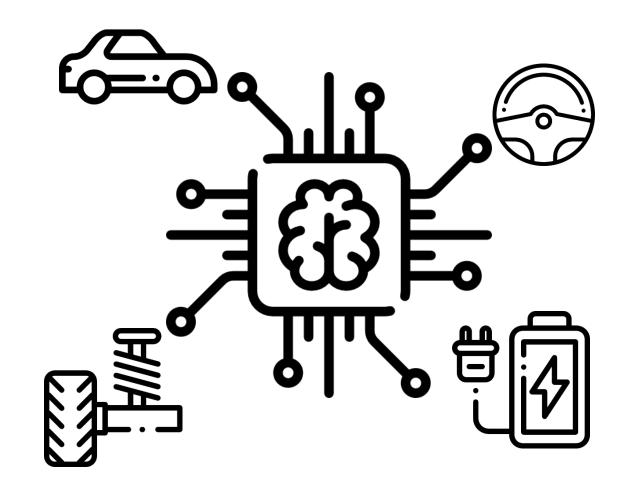
## **Artificial Intelligence in Automotive Technology**

Johannes Betz / Prof. Dr.-Ing. Markus Lienkamp / Prof. Dr.-Ing. Boris Lohmann



#### **Lecture Overview**

<b>Overall Introduction for the Lecture</b> 18.10.2018 – Betz Johannes	6 Pathfinding: From British Museum to A* 29.11.2018 – Lennart Adenaw	<b>11 Reinforcement Learning</b> 17.01.2019 – Christian Dengler		
1 Introduction: Artificial Intelligence	P6:	P11		
18.10.2018 – Betz Johannes	29.11.2018 – Lennart Adenaw	17.01.2019 – Christian Dengler		
P1:	7 Introduction: Artificial Neural Networks	12 AI-Development		
18.10.2018 – Betz Johannes	06.12.2018 – Lennart Adenaw	24.01.2019 – Johannes Betz		
2 Perception	P7	P12		
25.10.2018 – Betz Johannes	06.12.2018 – Lennart Adenaw	24.01.2019 – Johannes Betz		
P2:	8 Deep Neural Networks	13 Free Discussion		
25.10.2018 – Betz Johannes	13.12.2018 – Jean-Michael Georg	31.01.2019 - Betz/Adenaw		
3 Supervised Learning: Regression	P8			
08.11.2018 – Alexander Wischnewski	13.12.2018 – Jean-Michael Georg			
P3:	9 Convolutional Neural Networks			
08.11.2018 – Alexander Wischnewski	20.12.2018 – Jean-Michael Georg			
4 Supervised Learning: Classification	P9			
15.11.2018 – Jan-Cedric Mertens	20.12.2018 – Jean-Michael Georg			
P4:	10 Recurrent Neural Networks			
15.11.2018 – Jan-Cedric Mertens	10.01.2019 – Christian Dengler			
5 Unsupervised Learning: Clustering	P10			
22.11.2018 – Jan-Cedric Mertens	10.01.2019 – Christian Dengler			

Depth of understanding

## **Objectives of the lecture 10**

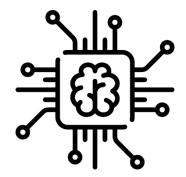
	Depth of understanding				
1. Make clear when to use Recurrent Neural	Remember	Understand	Utilize	Analyze	Estimate Develop
Networks (RNN) instead of static Neural Networks.					
2. Show the basic methods to train a RNN.					
3. Clarify problems that might occur when training a RNN over long sequences, and how they can be avoided/reduced.					
4. Give a short overview of different architectures for RNNs with use cases.					

Recurrent Neural Networks Johannes Betz / Prof. Dr. Markus Lienkamp / Prof. Dr. Boris Lohmann (Christian Dengler, M. Sc.)

#### Agenda

- 1. Sequential Data and Use Cases
- 2. Simple RNN and Backpropagation through Time
- 3. Challenge of long Term Dependencies
- 4. Advanced RNN Structures
- 5. Recurrent Neural Networks for Automobiles





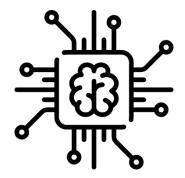
Recurrent Neural Networks Johannes Betz / Prof. Dr. Markus Lienkamp / Prof. Dr. Boris Lohmann (Christian Dengler, M. Sc.)

#### Agenda

#### **1. Sequential Data and Use Cases**

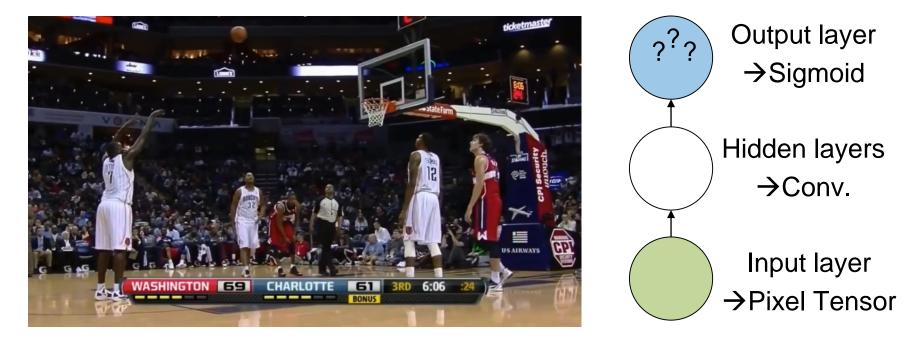
- 2. Simple RNN and Backpropagation through Time
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Sequential Data



#### Will he score?

Sequential Data



Will he score?

Sequential Data



Will he score?



Sequential Data



# Can I pass, should I break?



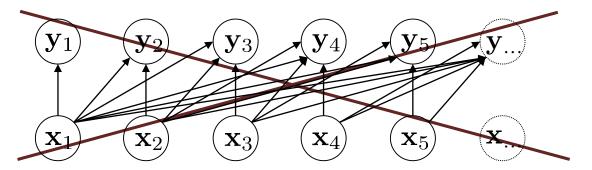
Sequential Data



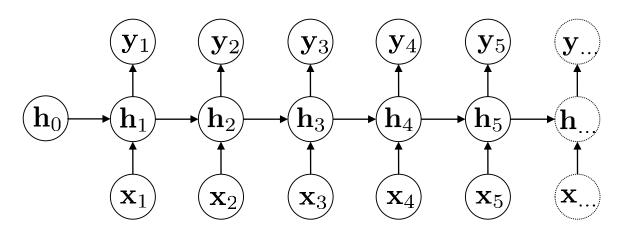




Fully connected model:



Single time-step update:



Use cases

- Speech recognition and generation
- Music recognition and generation
- Translation
- Image Capturing
- Video Capturing
- Modeling dynamics of physical systems

• ...



Image Classification and Generation [12]





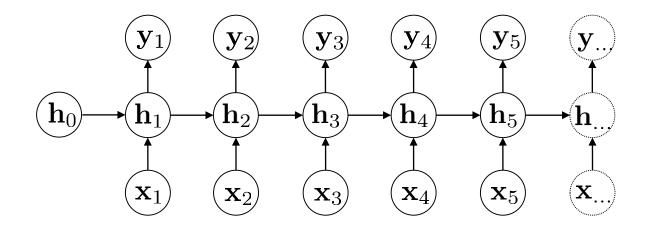
Image Classification and Generation [12]



#### Wrap up

- Often one observation does not contain the required information.
- The information is often hidden in sequences of data, but just taking a whole sequence as input will require too many parameters

 $\rightarrow$ Share parameters and add a memory to capture the important features of the past.



Recurrent Neural Networks Johannes Betz / Prof. Dr. Markus Lienkamp / Prof. Dr. Boris Lohmann (Christian Dengler, M. Sc.)

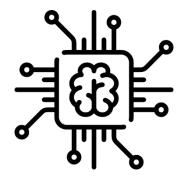
#### Agenda

1. Sequential Data and Use Cases

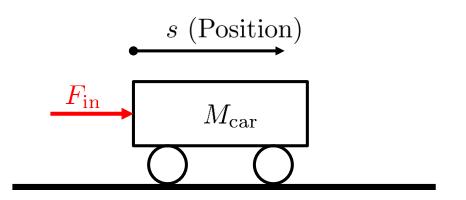
#### 2. Simple RNN and Backpropagation through Time

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Dynamical Systems in Engineering



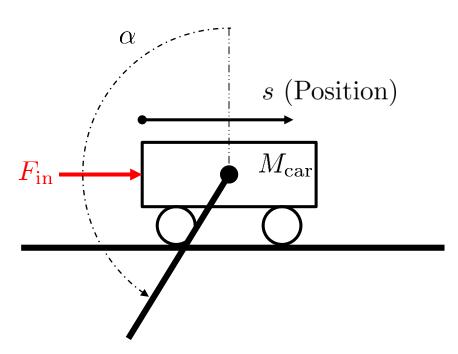
Input  $u = F_{in}$ , output y = s.

Model equations

linear state-space representation



Dynamical Systems in Engineering



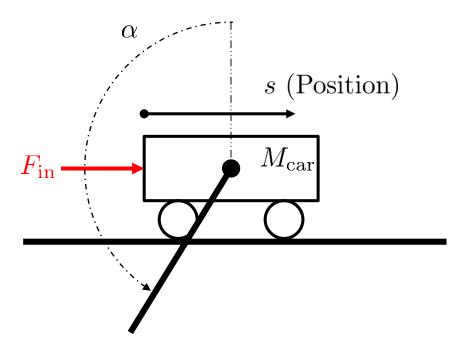
Model equations [16]:  $(M_{\text{cart}} + M_{\text{link}})\ddot{s} - M_{\text{link}}l_{\text{link}}\ddot{\alpha}\sin(\alpha) = F$ 

$$l_{\rm link}\ddot{\alpha} - g\sin(\alpha) = \ddot{s}\cos(\alpha)$$

 $M_{\rm link}, l_{\rm link}$ 



Dynamical Systems in Engineering



Nonlinear state-space model:

$$\begin{bmatrix} \dot{s} \\ \ddot{s} \\ \dot{\alpha} \\ \ddot{\alpha} \end{bmatrix} = \begin{bmatrix} \dot{s} \\ f_1(\dot{s}, \alpha, \dot{\alpha}, F) \\ \dot{\alpha} \\ f_2(\dot{s}, \alpha, \dot{\alpha}, F) \end{bmatrix}$$
$$y = s$$

 $M_{\rm link}, l_{\rm link}$ 

Dynamical Systems in Engineering

Continuous-time system:

$$\begin{split} \dot{\mathbf{x}} &= \mathbf{f}(\mathbf{x}, \mathbf{u}) \\ \mathbf{y} &= \mathbf{g}(\mathbf{x}) \end{split}$$

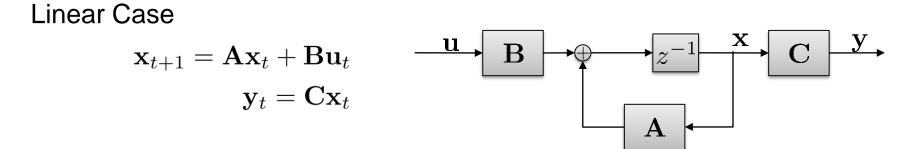
Forward Euler Runge-Kutta 4 ...

Discrete-time system:

$$\mathbf{x}_{t+1} = \tilde{\mathbf{f}}(\mathbf{x}_t, \mathbf{u}_t)$$
  
 $\mathbf{y}_t = \mathbf{g}(\mathbf{x}_t)$ 



Dynamical Systems in Engineering



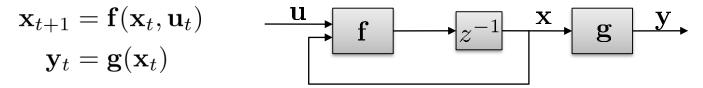
Nonlinear Case

$$\mathbf{x}_{t+1} = \mathbf{f}(\mathbf{x}_t, \mathbf{u}_t) \qquad \qquad \mathbf{u} \qquad \mathbf{f} \qquad \mathbf{z}^{-1} \qquad \mathbf{x} \qquad \mathbf{g} \qquad \mathbf{y} \qquad \mathbf{g} \qquad \mathbf{g} \qquad \mathbf{y} \qquad \mathbf{g} \qquad$$

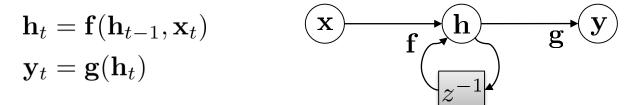


Notation

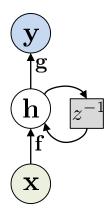
Engineering, e.g. Control Theory



Machine Learning



Notation



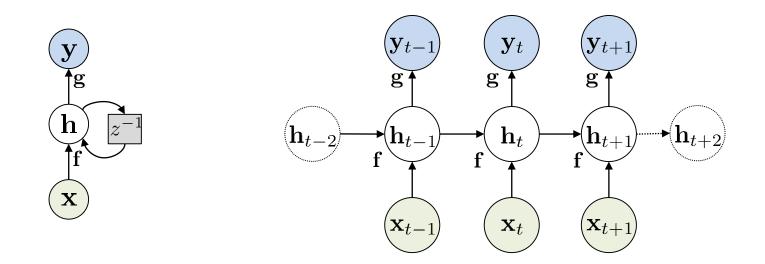
Symbol	Meaning
x	Input
h	Hidden state
У	Output
$\hat{\mathbf{y}}$	Observation/Data



Unfolding the graph

Dynamical system:

$$\mathbf{h}_t = \mathbf{f}(\mathbf{h}_{t-1}, \mathbf{x}_t)$$
$$\mathbf{y}_t = \mathbf{g}(\mathbf{h}_t)$$



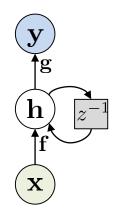


Unfolding the graph

Dynamical system:

$$\mathbf{h}_t = \mathbf{f}(\mathbf{h}_{t-1}, \mathbf{x}_t)$$
$$\mathbf{y}_t = \mathbf{g}(\mathbf{h}_t)$$

Evalute/Simulate RNN (Inference) :

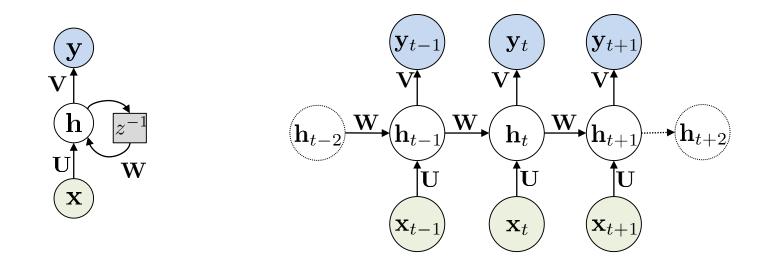




Unfolding the graph

Dynamical system:

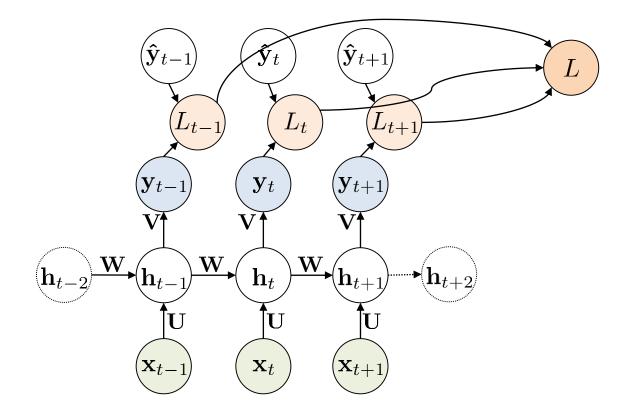
$$h_t = \tanh(\mathbf{W}h_{t-1} + \mathbf{U}\mathbf{x}_t + \mathbf{b})$$
$$\mathbf{y}_t = \mathbf{V}h_t + \mathbf{v}$$





**Optimization setting** 

Loss function as a sum over timesteps:  $L = \sum_t L_t = \sum_t L(\mathbf{y}_t, \hat{\mathbf{y}}_t)$ 





Loss Function

As for static Neural Networks: minimize the cross-entropy between the generating distribution and our model P.

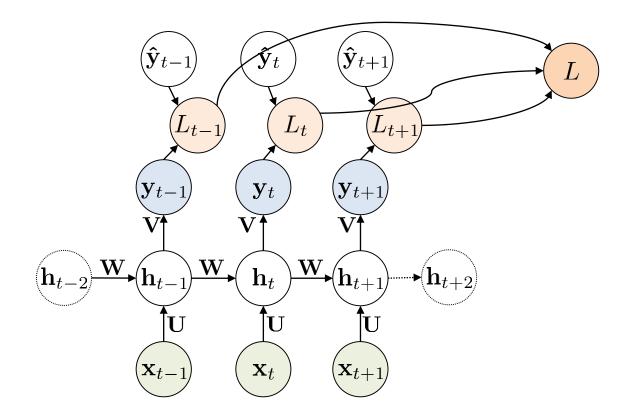
$$L_t = -\log P(o_t = y_t | x_t, x_{t-1}, \dots, x_1, h_0)$$

E.g. for a normal distribution  $\mathcal{N}(\mu(x_t, x_{t-1}, \dots, x_1, h_0), 1^2)$  we restore the quadratic loss function

$$L_t = \frac{1}{2} \left( y_t - \mu(x_t, \dots) \right)^2$$

Backpropagation through time (BPTT)

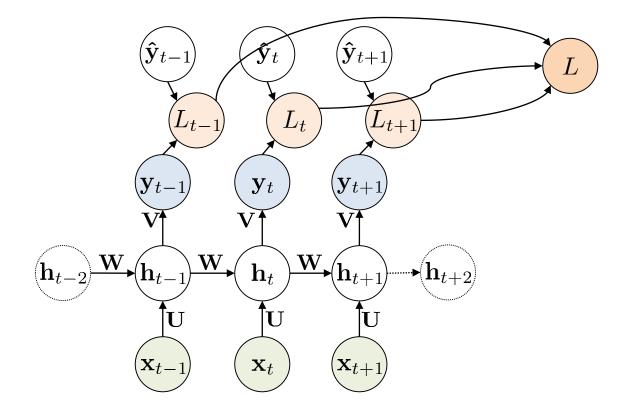
Backpropagation, applied to the unfolded graph of a sequence.



Backpropagation through time (BPTT)

Backpropagation, applied to the unfolded graph of the sequence.

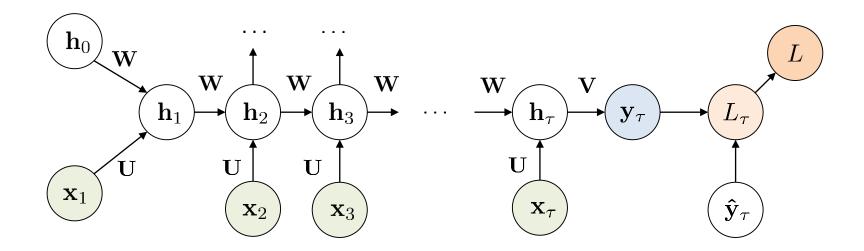
 $\frac{\partial}{\partial W^T}L = \frac{\partial L}{\partial h^{\tau,T}}\frac{\partial h^{\tau}}{\partial W^T} + \frac{\partial L}{\partial h^{\tau-1,T}}\frac{\partial h^{\tau-1}}{\partial W^T} + \frac{\partial L}{\partial h^{\tau-2,T}}\frac{\partial h^{\tau-2}}{\partial W^T} + \dots$ 





Backpropagation through time (BPTT)

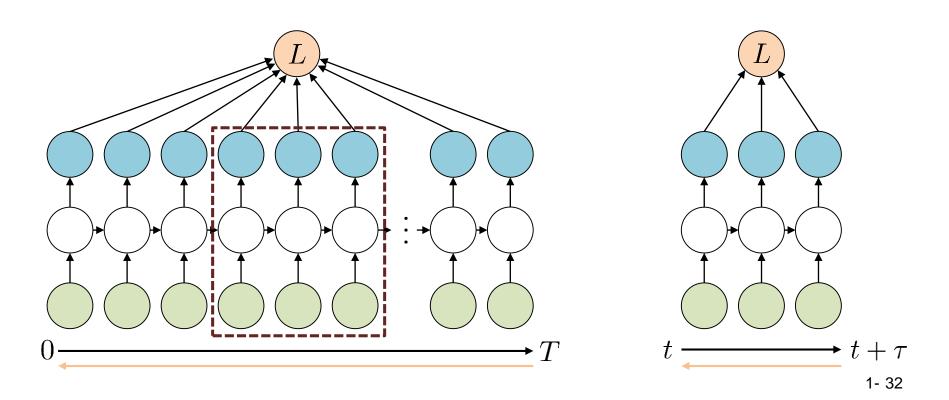
Similar to a deep neural network, with the number of layers increasing with the number of timesteps (deep computation graph).





Truncated Backpropagation through time

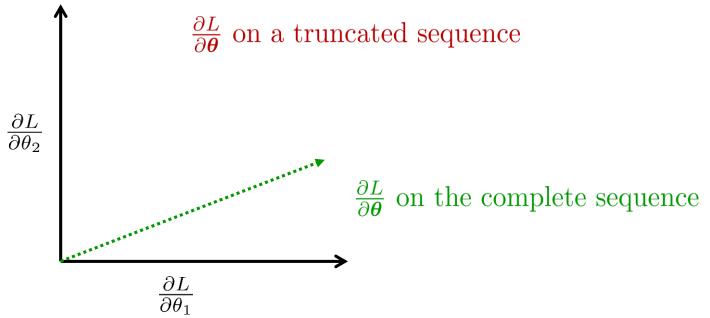
Backpropagation, applied to the unfolded graph of a chunk of the sequence of length  $\tau$ . Similar to minibatches in supervised learning.





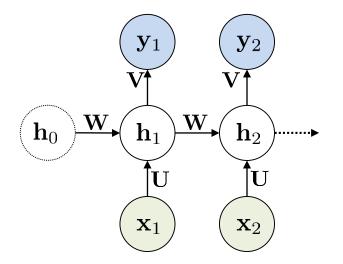
Truncated Backpropagation through time

Truncated Backpropagation through time is biased! Unbiased versions e.g. in [1].



State initialization

How can we chose  $h_0$ ?

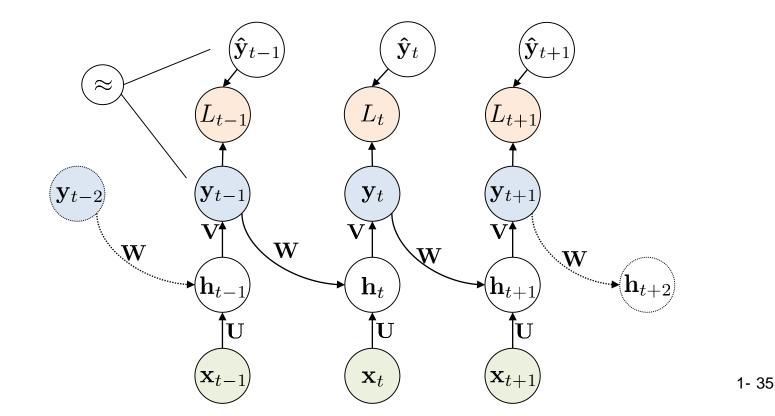


- Initialize as zero [2]
- Noisy zero mean [5]
- Treat as parameter to learn [6]
- Initialize using a second Neural Network [3]



Feedback of the output

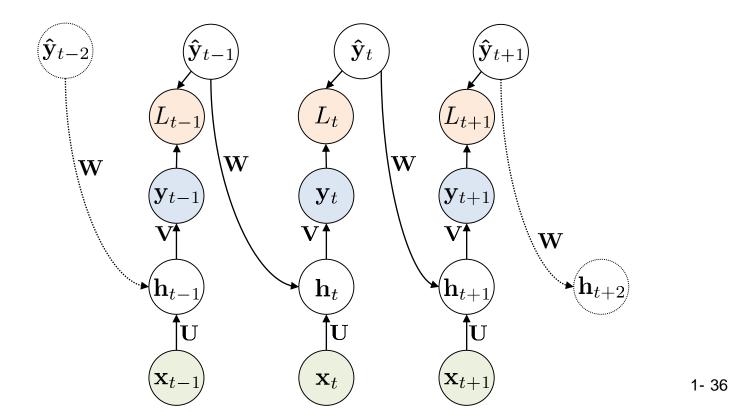
Feedback of the **output**. We can split the computation graph by using the target values from the data  $\rightarrow$  supervised learning





**Teacher forcing** 

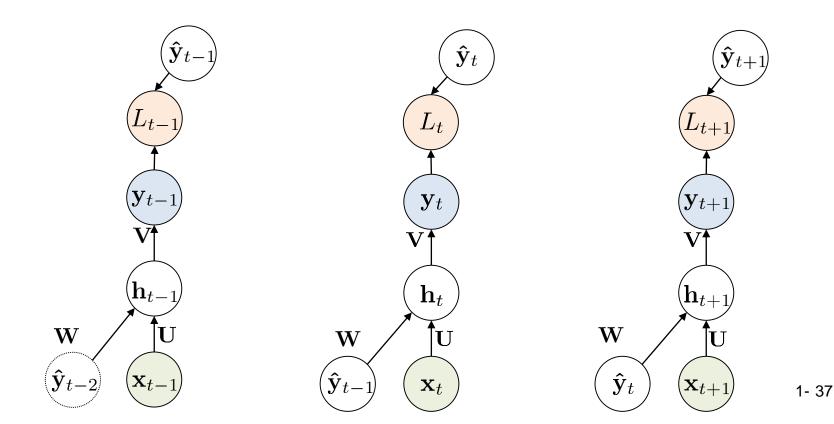
Feedback of the **output**. We can split the computation graph by using the target values from the data  $\rightarrow$  supervised learning





**Teacher forcing** 

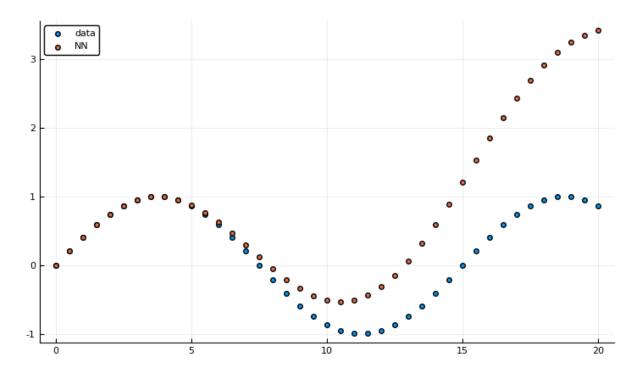
Feedback of the **output**. We can split the computation graph by using the target values from the data  $\rightarrow$  supervised learning





**Teacher forcing** 

#### Problem with accumulating errors when sampling longer sequences.

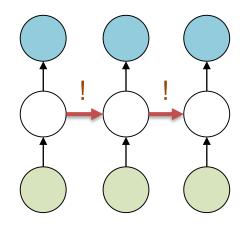




Regularization using Dropout

Problematic when used on shared weights

- Regularize non-shared parameter only
- Sample one dropout pattern for the shared parameters and reuse it for the timesteps in the minibatch





Wrap up

- A RNN is just a state-space model with free parameters that we want to learn.
- Gradient descend using backpropagation as usual, but:
  - Computation graph deep (need to store and compute a lot)
     -> use truncated sequences
  - But truncated sequences lead to **bias** in the gradient
- If we use output as input again, we can use teacher forcing
   -> no need to backpropagate over sequences

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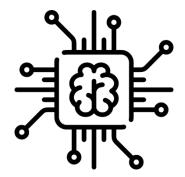
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Vanishing or exploding Gradients

Suppose we have a recurrent function

$$h_{t+1} = h_{t+k} = \frac{\partial h_{t+k}}{\partial h_t} =$$

For long sequences

$$\lim_{k \to \infty} \frac{\partial h_{t+k}}{\partial h_t} =$$

Vanishing or exploding Gradients

$$\mathbf{h}_{t+1} = \tanh(\mathbf{W}\mathbf{h}_t + \mathbf{U}\mathbf{x}_t + \mathbf{b})$$
$$\mathbf{y}_t = \mathbf{V}\mathbf{h}_t + \mathbf{v}$$

For backpropagation we need

 $\frac{\partial L_{t+k}}{\partial \mathbf{h}_t^T} = \frac{\partial L_{t+k}}{\partial \mathbf{h}_{t+k}^T} \frac{\partial \mathbf{h}_{t+k}}{\partial \mathbf{h}_t^T}$ 

$$\frac{\partial \mathbf{h}_{t+1}}{\partial \mathbf{h}_t^T} = \operatorname{diag}(1 - \mathbf{h}_{t+1} \odot \mathbf{h}_{t+1}) \mathbf{W}$$

Vanishing or exploding Gradients

For matrices, we need to look at the spectral norm = largest singular value

$$\gamma = \max \left\| \operatorname{diag}(1 - \tanh(\dots)^2) \right\|$$

One can show that

$$\left\|\frac{\partial \mathbf{h}_{t+1}}{\partial \mathbf{h}_t^T}\right\| \le \|\gamma \mathbf{W}\|$$
$$\left\|\frac{\partial \mathbf{h}_{t+k}}{\partial \mathbf{h}_t^T}\right\| \le \|\gamma \mathbf{W}\|^k$$

Vanishing or exploding Gradients

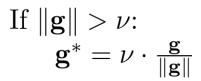
We want

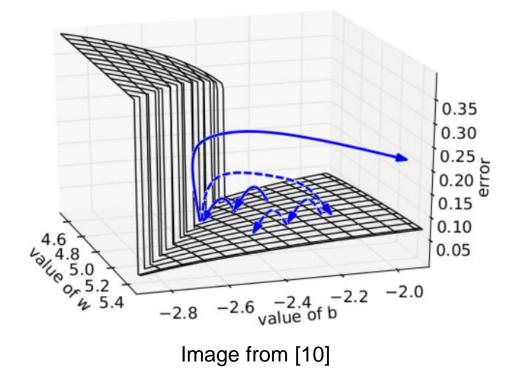
$$\left\|\frac{\partial \mathbf{h}_{t+k}}{\partial \mathbf{h}_t^T}\right\| \le \left\|\gamma \mathbf{W}\right\|^k \approx 1$$

We know  $\gamma$ , so initializing W using a good distribution helps at the beginning of the training.

Exploding gradient, Gradient clipping

If gradient is to big, use only the direction, not the magnitude.

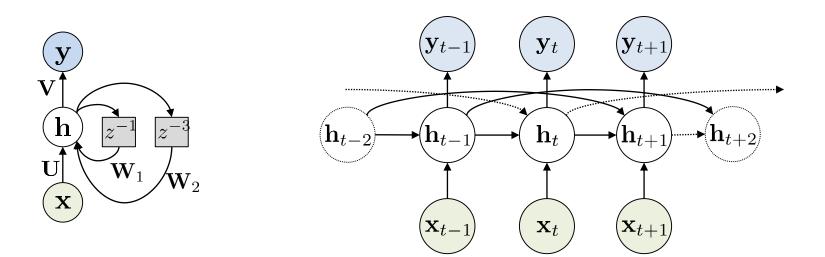






Vanishing Gradient, Skip Connections

"Jump over" iterative gradients



Today: use different parameterization, e.g. gated network

#### Wrap up

- Reusing the same weights can lead to very big or very small gradients that can slow down training.
- Big gradients should be diminished in some way, e.g. cut norm, cut single entires
- Small gradients can be tackled by using inputs from multiple steps in the past
- Good initialization of the recurrent weights can avoid small or big gradients at the beginning of the training.

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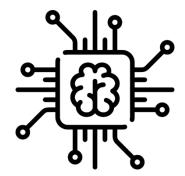
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#### 4. Advanced RNN Structures

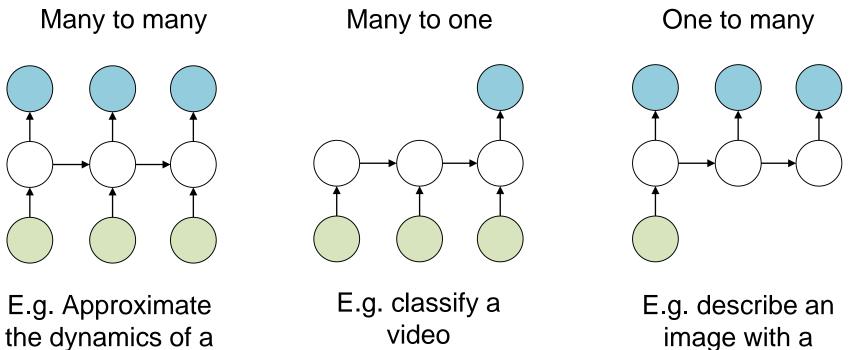
5. Recurrent Neural Networks for Automobiles







Input – Output relations



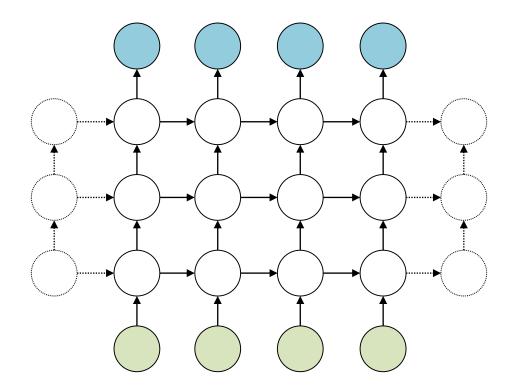
physical system

video

1-50

sentence

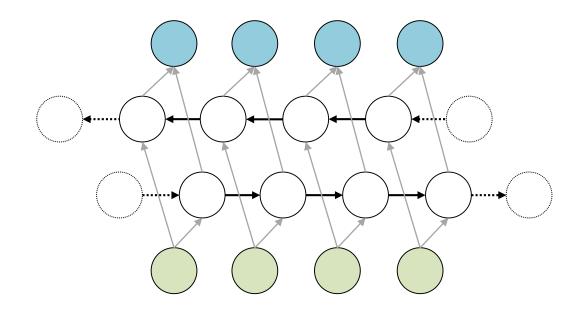
Multilayer RNN



Short analysis of the influence of multiple layers in [11]

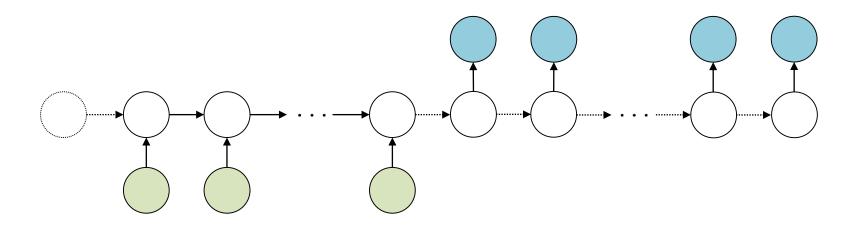
**Bidirectional RNN [4]** 

Including future information can be helpful. E.g. handwriting recognition.



Sequence to sequence [7]

- 1) A sequence is encoded by a RNN with parameters  $\mathbf{W}_1$
- 2) The information is decoded by RNN with parameters  $\mathbf{W}_2$
- E.g. translation into different languages.

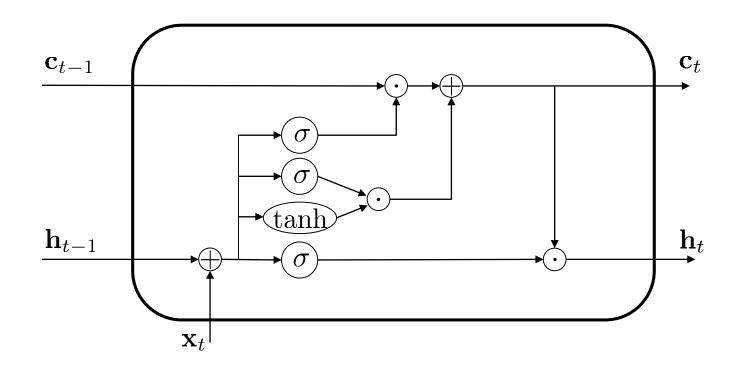


Long short-term memory (LSTM) [8]

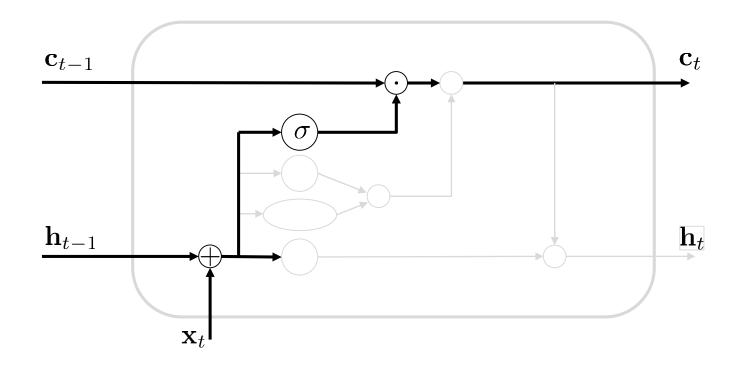
- Idea of not updating the whole hidden state each time
- Protect the state from being overwritten by useless information
- Be selective in
  - What to write (input gate)  $\mathbf{i}_t = \sigma(\mathbf{W}_i \mathbf{h}_{t-1} + \mathbf{U}_i \mathbf{x}_t + \mathbf{b}_i)$
  - What to read (output gate)  $\mathbf{o}_t = \sigma (\mathbf{W}_o \mathbf{h}_{t-1} + \mathbf{U}_o \mathbf{x}_t + \mathbf{b}_o)$
  - What to forget (forget gate)  $\mathbf{f}_t = \sigma(\mathbf{W}_f \mathbf{h}_{t-1} + \mathbf{U}_f \mathbf{x}_t + \mathbf{b}_f)$

$$\mathbf{c}_t = \mathbf{f}_t \odot \mathbf{c}_{t-1} + \mathbf{i}_t \odot \tanh(\mathbf{W}_h \mathbf{h}_{t-1} + \mathbf{U}_h \mathbf{x}_t + \mathbf{b}_h)$$
$$\mathbf{h}_t = \mathbf{o}_t \odot c_t$$

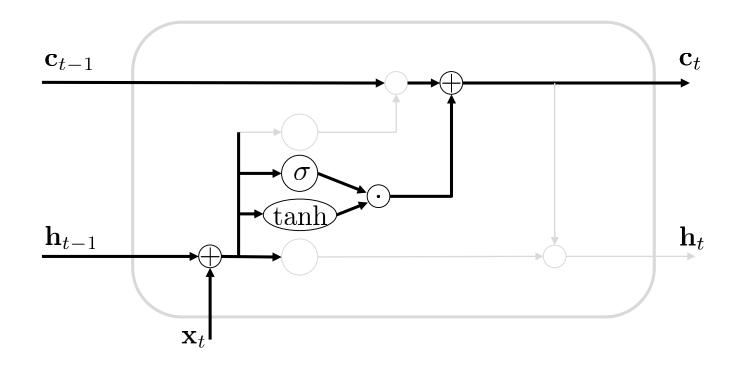
LSTM Structure



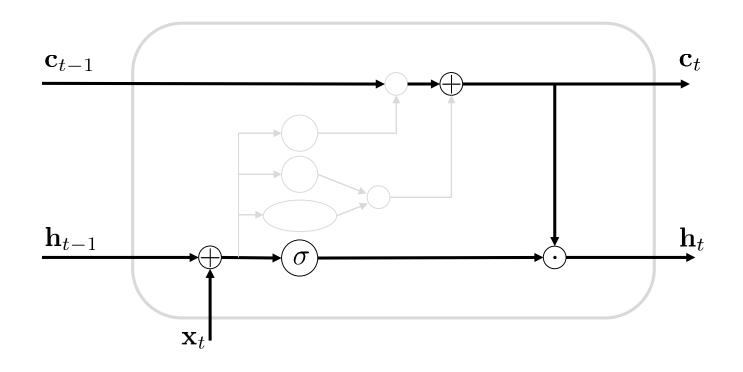
LSTM, forget



LSTM, input

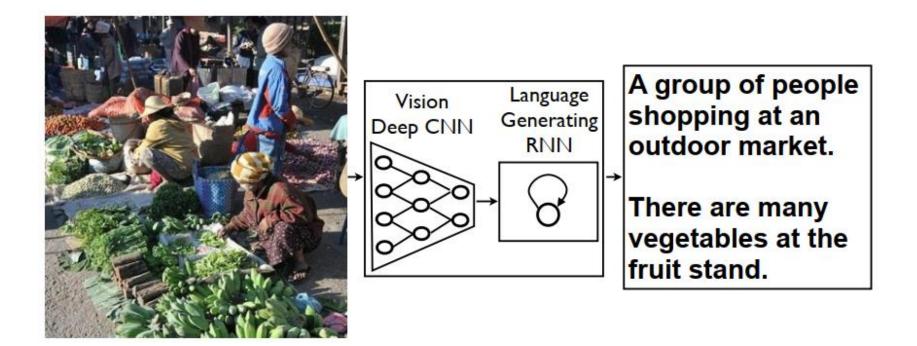


LSTM, output



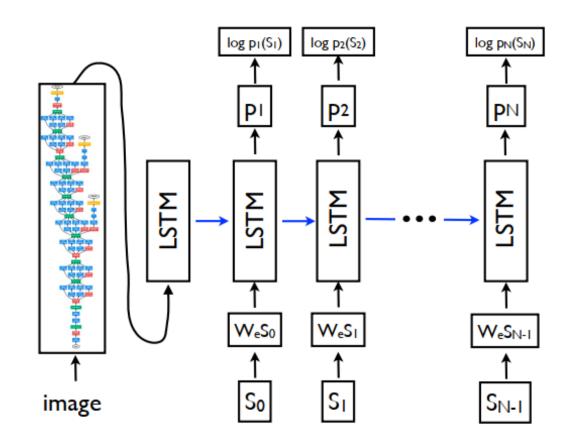


LSTM example in Vinyals et al. [9]





LSTM example in [9]



A person riding a motorcycle on a dirt road.



A group of young people playing a game of frisbee.



A herd of elephants walking across a dry grass field.



Two dogs play in the grass.



Two hockey players are fighting over the puck.



A close up of a cat laying on a couch.



A skateboarder does a trick



A little girl in a pink hat is blowing bubbles.



A red motorcycle parked on the



A dog is jumping to catch a



A refrigerator filled with lots of food and drinks.



A yellow school bus parked in a parking lot.



**Describes without errors** 

**Describes with minor errors** 

Somewhat related to the image

Unrelated to the image

LSTM example in [9]

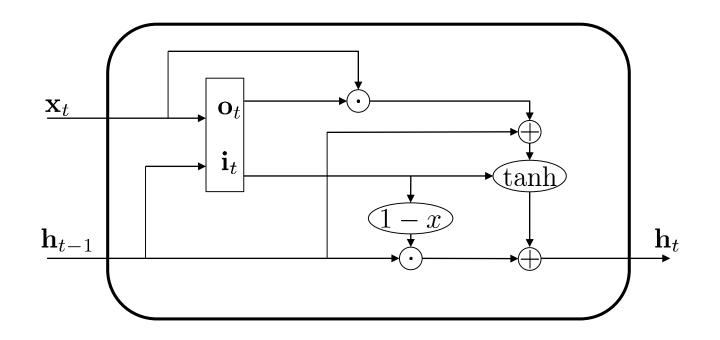
Gated Recurrent Unit (GRU)

- Same idea using gates, here
  - Input/write  $\mathbf{i}_t = \sigma(\mathbf{W}_i \mathbf{h}_{t-1} + \mathbf{U}_i \mathbf{x}_t + \mathbf{b}_i)$
  - Forget  $\mathbf{f}_t = 1 \mathbf{i}_t$
  - Output/read  $\mathbf{o}_t = \sigma(\mathbf{W}_o \mathbf{h}_{t-1} + \mathbf{U}_o \mathbf{x}_t + \mathbf{b}_o)$

 $\mathbf{h}_{t+1} = (1 - \mathbf{i}_t) \odot h_{t-1} + \mathbf{i}_t \odot \tanh(\mathbf{W}_h \mathbf{h}_{t-1} + \mathbf{U}_h (\mathbf{o}_t \odot \mathbf{x}_t) + \mathbf{b}_h)$ 

Read first then write!

**GRU Structure** 



Wrap up

- Many structures and activations possible: deep RNN, bidirectional RNN, sequence to sequence, LSTM-cells, GRU,...
- Hard to know a priori what will work best. Currently LSTM and GRU used a lot.

# Wrap up

- Recurrent Neural Network = Dynamical System
- Common use cases: Wherever data appears in sequences, e.g. audio, video, text, language...
- Unfolding in time is simular to training deep neural network, but additional difficulties appear: deep computation graph, initial state, biased gradient, gradients small or large...
- Different RNN structures might be favorable for different situations: bidirection RNN, sequence to sequence, gated networks...
- No "one fits all" solution, still topic of research.

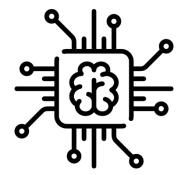
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- 1. Sequential Data and Use Cases
- 2. Simple RNN and Backpropagation through Time
- 3. Challenge of long Term Dependencies
- 4. Advanced RNN Structures

#### **5. Recurrent Neural Networks for Automobiles**







#### Recurrent neural networks for driver activity anticipation via sensory-fusion architecture Jain, A.; Singh, A.; Koppula, H. S.; Soh, S. & Saxena, A. 2016 IEEE International Conference on Robotics and Automation (ICRA), **2016**

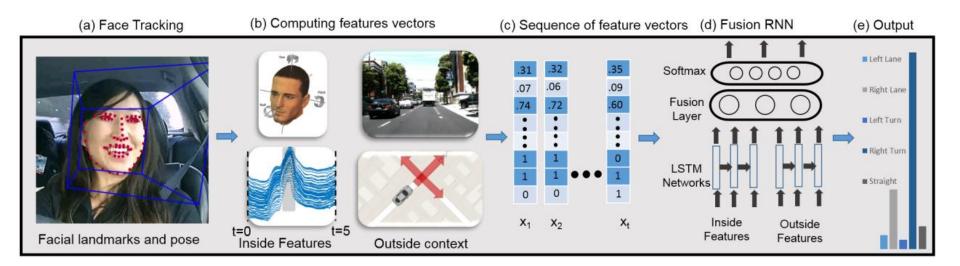


#### Maneuver anticipation

Predict the drivers action multiple seconds ahead.

→multiple sensors and LSTM's fused

Recurrent neural networks for driver activity anticipation via sensory-fusion architecture



- Multiple LSTM, one for each sensor (camera, GPS, vehicle dynamics,...)
- Sensor fusion on hidden states as fully connected
- Loss function with increased loss in late predictions



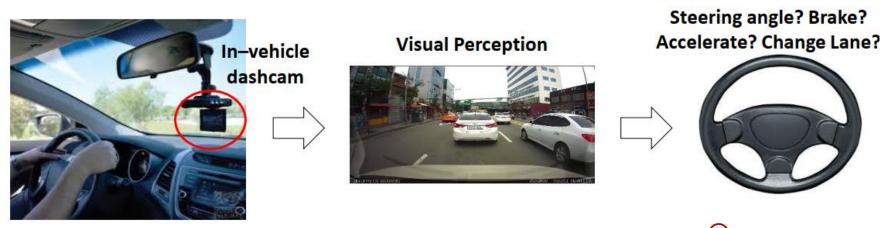
Recurrent neural networks for driver activity anticipation via sensory-fusion architecture

		Lane change			Turns		
]	Method	Pr (%)	Re (%)	Time-to- maneuver (s)	Pr (%)	Re (%)	Time-to- maneuver (s)
	Chance	33.3	33.3	-	33.3	33.3	-
	SVM 27	$73.7 \pm 3.4$	$57.8 \pm 2.8$	2.40	$64.7 \pm 6.5$	$47.2 \pm 7.6$	2.40
	Random-Forest	$71.2 \pm 2.4$	$53.4 \pm 3.2$	3.00	$68.6 \pm 3.5$	$44.4 \pm 3.5$	1.20
	IOHMM [19]	$81.6 \pm 1.0$	$79.6 \pm 1.9$	3.98	$77.6 \pm 3.3$	$75.9 \pm 2.5$	4.42
	AIO-HMM 19	$83.8 \pm 1.3$	$79.2 \pm 2.9$	3.80	$80.8\pm3.4$	$75.2\pm2.4$	4.16
	S-RNN	$85.4 \pm 0.7$	$86.0 \pm 1.4$	3.53	$75.2 \pm 1.4$	$75.3 \pm 2.1$	3.68
Our	F-RNN-UL	<b>92.7</b> ± 2.1	$84.4 \pm 2.8$	3.46	$81.2 \pm 3.5$	$78.6\pm2.8$	3.94
Methods	F-RNN-EL	$88.2 \pm 1.4$	<b>86.0</b> ± 0.7	3.42	<b>83.8</b> ± 2.1	<b>79.9</b> ± 3.5	3.78

 Comparison of different modifications, and also comparison with other works.



#### Deep steering: Learning end-to-end driving model from spatial and temporal visual cues Chi, L. & Mu, Y. *arXiv preprint*, **2017**

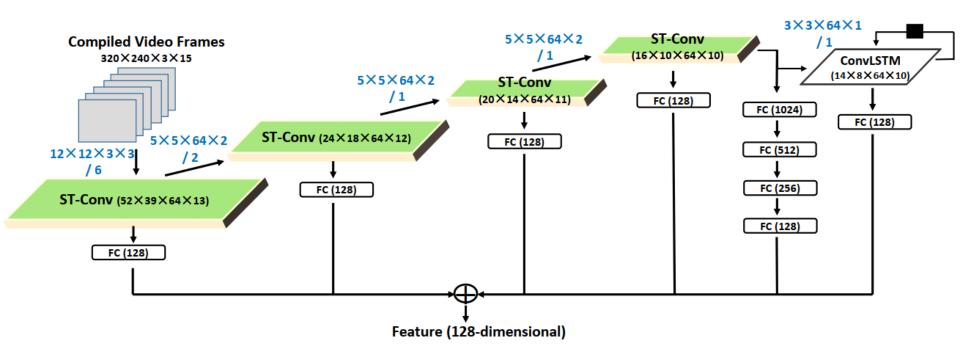


Only prediction in the paper, no driving 😕



Deep steering: Learning end-to-end driving model from spatial and temporal visual cues

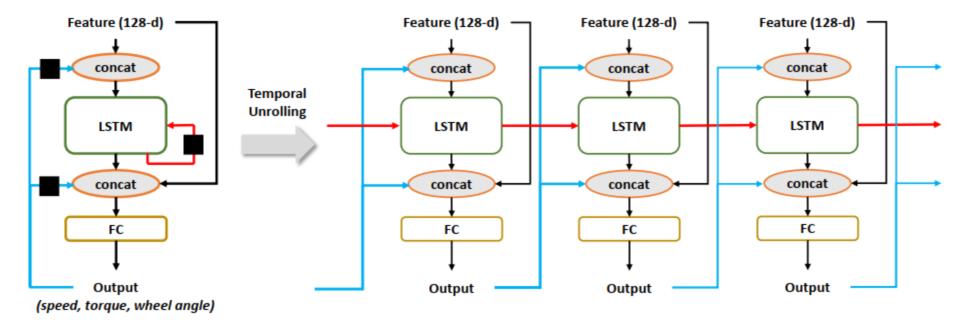
#### "Feature extraction sub-network"





Deep steering: Learning end-to-end driving model from spatial and temporal visual cues

# "Steering-prediction sub-network"





Deep steering: Learning end-to-end driving model from spatial and temporal visual cues



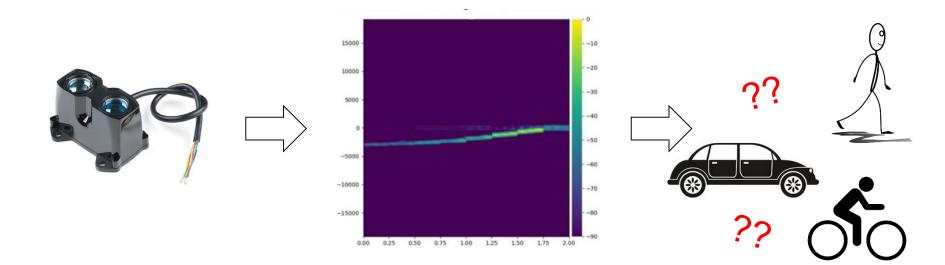




#### Practical classification of different moving targets using automotive radar and deep neural networks

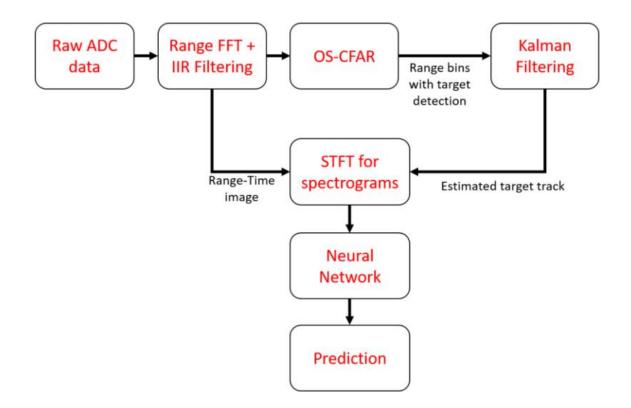
Angelov, A.; Robertson, A.; Murray-Smith, R. & Fioranelli, F.

IET Radar, Sonar & Navigation, IET, 2018





Practical classification of different moving targets using automotive radar and deep neural networks





Practical classification of different moving targets using automotive radar and deep neural networks

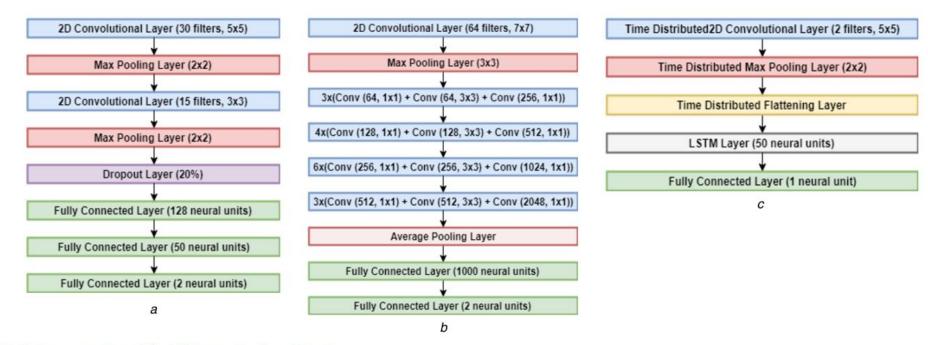


Fig. 3 Representation of the different network architectures

(a) Convolutional neural network similar to VGG type, (b) Convolutional residual network, (c) Combination of convolutional and recurrent LSTM network



Practical classification of different moving targets using automotive radar and deep neural networks

Table 3         Test accuracy for two network architectures           evaluated on three class problems							
Evaluation/	VGG-like	VGG-like	CNN-	CNN-			
network type	CNN (2 s	CNN (0.5 s	LSTM (2 s	LSTM (0.5			
	long datasets)	long datasets)	long datasets)	s long datasets)			
car-person- bicycle classification	79%	83%	93%	83%			
car-person-2 people classification	81%	78%	80%	84%			

Table 4	Test accuracy for three types of networks (VGG-			
like, CNN-LSTM, and VGG-LSTM) on all considered				
problems, with regularisation and batch normalisation				

Evaluation/	VGG-like	VGG-like	CNN-	CNN-
network type	CNN (2 s	CNN (0.5 s	LSTM (2 s	LSTM
	long	long	long	(0.5 s long
	datasets)	datasets)	datasets)	datasets)
car-person- bicycle classification	78.6%	81.1%	50%	73.5%
car-person-2 people classification	77.8%	88.6%	44.4%	78.3%
all-4-classes- classification (VGG LSTM)	_	_	—	70%



#### **Evaluation**



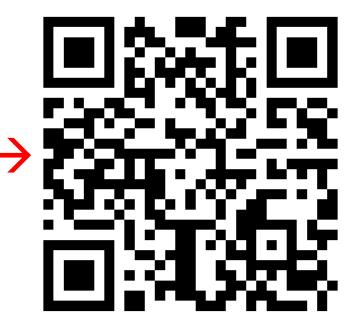
# **Evaluation**

- In this lecture we are doing in regularly evaluation of each lecture
- We want **your** feedback for every **individual** lecture
- We evaluate the lecture each week
- We give feedback based on the evaluation the week after



## **Evaluation – Step by Step**

- 1. Get out your smartphones
- 2. Open an app for QR-code Reading
- 3. Read the following QR-code on the right side
- 4. Open the website
- 5. Answer the questions
- 6. Send the evaluation



### OR

- 1. Open the following website in your browser: <u>https://evasys.zv.tum.de/evasys/online.php?p=AIAT-10</u>
- 2. Answer the questions
- 3. Send the evaluation

# A.1. Literature

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